

List of talks for the seminar

# Local Langlands Correspondence for $GL(2)$

## part II

— winter term 2008–2009, Do 14–16, SR D —

All §x.y without further reference refer to [BH06]. An \* marks talks which rely partly on part 1 of the seminar.

1. DOMINIK KLEIN

**Analysis on locally pro-finite groups.** Compactly supported functions, Haar measure, Haar integral, modulus character, unimodular groups §3.1-3; duality for (compactly-) induced representations §3.4+5.

2. LENNART MEIER

**The Hecke algebra.** Hecke algebra §4.1; smooth modules versus smooth representations §4.2; action of  $K$ -biinvariant functions on the set of  $K$ -invariants §4.3; separation property §4.4; spherical Hecke algebra and intertwining §11.1 Definition + Proposition 2, §11.2-3.

3. MARTIN KREIDL

**The mirabolic group.** Representation theory of the unipotent radical of the Borel  $N \cong (F, +)$  §8.1; representation theory of the mirabolic group §8.2+3.

4. ULRICH TERSTIEGE

**The Jacquet module.** The Jacquet module and principal series representations §9.1; Restriction-Induction Lemma §9.3; projection formula §9.5 (9.5.2); composition series of parabolic induced representations for  $GL_2(F)$ , irreducibility criterion, Classification Theorem of principal series representations §9.6–11.

5. PHILIPP HARTWIG

**Matrix coefficients.** Matrix coefficients §10.1; dichotomy: principal series (subrepresentation of some  $\text{Ind}_B^G(\chi)$ ) versus cuspidal representations (matrix coefficients are compactly supported modulo the center) §10.2; irreducible representations are admissible (zulässig) §9.4 + §10.1; the compactly induced representations from cuspidal types<sup>1</sup> are cuspidal §11.4<sup>2</sup>.

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<sup>1</sup>No details about cuspidal types required. One only needs to know that all of these representations are shown to be irreducible by theorem §11.4

<sup>2</sup>First part of the proof of Theorem 11.4

6. PETER SCHOLZE

**The Exhaustion Theorem\***. The exhaustion theorem, irreducible representations with Iwahori fixed vector §14, §17.1–3.

7. TIMO RICHARZ

**Analysis on  $GL_1(F)$** . Fourier transform, inversion formula §23.1, zeta function of a compactly supported function,  $L$ -function, functional equation §23.2+3, Tate local  $\varepsilon$ -factors, Tate’s local functional equation, behaviour of local  $\varepsilon$ -factors under unramified twist and change of additive character §23.4, §23.5 Lemma 1.

8. EUGEN HELLMANN

**Analysis on  $GL_2(F)$** . Fourier transform, zeta function, Godement–Jacquet functional equation, Godement–Jacquet local  $\varepsilon$ -factor, behaviour of local  $\varepsilon$ -factors under unramified twist and change of additive character §24.1–5; proof of the Godement–Jacquet functional equation for cuspidal representations §24.6+7.

9. ALEXANDER IVANOV

**Gauß sums and stability theorem.\***  $GL_1$ -case: Gauß sums, stability theorem §23.5 Theorem 1, §23.6+7;  $GL_2$ -case: nonabelian Gauß sums, stability theorem §25.

10. OLIVER LORSCHIED

**Proof of the functional equation for principal series** Essentially square integrable representations, discrete series §17.4–10<sup>3</sup>; The Godement–Jacquet functional equation for principal series representations §26.

11. EVA VIEHMANN

**The Converse Theorem.** The Converse Theorem, characterisation of cuspidal representations by trivial  $L$ -functions of all twists §27.

12. NN.

**Local  $\varepsilon$ -functions for Galois representations.** Langlands–Deligne local  $\varepsilon$ -factors, formulas for local  $\varepsilon$ -factors under unramified twist and change of additive character, stability formula, functional equation §29.

Inducing constants, Brauer Induction Theorem, inducing constants are determined by values on characters, global  $L$ -function, global functional equation and global  $\varepsilon$ -factor, construction of local Langlands–Deligne  $\varepsilon$ -factors from global approximation §30.

13. NN.

**Weil–Deligne representations.** Weil–Deligne representations, Artin  $L$ -function, local  $\varepsilon$ -factors, relation with  $\ell$ -adic representations, Grothendieck’s Monodromy Theorem, Frobenius semisimple representations §31, §32.

14. NN.

**The local Langlands Correspondence — comparison of  $L$ -function and  $\varepsilon$ -factors.** The Langlands constants §30.4; the Langlands Correspondence — complete proofs in the tame case §33, §34; the  $\ell$ -adic correspondence §35.

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<sup>3</sup>as needed for the rest

## Literatur

- [BH06] Bushnell, C. J., Henniart, G., *The local Langlands Conjecture for  $GL(2)$* , Grundlehren der Math. Wissenschaften **335**, Springer, 2006.
- [De73] Deligne, P., Les constantes des équations fonctionnelles des fonctions L, in *Modular functions of one variables II*, LNM **349**, Springer, 1973.
- [Se77] Serre, J.-P., *Linear representations of finite groups*, translated from the French edition *Représentations linéaires des groupes finis*, GTM **42**, Springer, 1977.
- [Se79] Serre, J.-P., *Local Fields*, translated from the French edition *Corps locaux*, GTM **67**, Springer, 1979.
- [Ta65] Tate, J. T., Fourier analysis in number fields, and Hecke's zeta-functions, in J. W. S. Cassels, A. Fröhlich (eds.), *Algebraic number theory*, Academic Press, 1967.
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- [We00] Wedhorn, T., The local Langlands correspondence for  $GL(n)$  over  $p$ -adic fields, arXiv:math.AG/0011210v2, 25 Nov 2000.